

# International Review of Biophysical Chemistry (IREBIC)

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# *International Review of Biophysical Chemistry* (IREBIC)

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# Orientalional Order within Biological Membranes

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**Abstract** – Recently developed approaches analyzing the degree of in-plane orientational ordering are compared. The first one originates from an intrinsic anisotropic shape of membrane constituents, based on which the mismatch curvature tensor  $\underline{M}$  is introduced. The second one originates from the nematic tensor order parameter  $\underline{Q}$  reflecting average local degree of orientational ordering. Based on these tensors free energy of systems are derived taking into account symmetry allowed combinations of tensors. From both approaches the degree of local orientational ordering is determined as a function of membrane shape. In the paper we discuss relevance of these approaches. **Copyright © 2012 Praise Worthy Prize S.r.l. - All rights reserved.**

**Keywords:** Vesicles, Orientalional Order, Topological Defects

## Nomenclature

$a_0$	Surface area of a membrane
$A_0, B, k$	Material constants
$\underline{C}$	The effective curvature tensor
$\underline{C}_m$	The intrinsic curvature tensor
$C_1, C_2$	The principal curvatures
$C_{1m}, C_{2m}$	The intrinsic principal curvatures
$D$	The curvature deviator
$D_m$	The intrinsic curvature deviator
$Det$	Determinant
$\vec{e}$	A temporal local orientation of a nanodomain
$\{\vec{e}_1, \vec{e}_2\}$	The unit vectors of $\underline{C}$ eigenframe
$\{\vec{e}_{1m}, \vec{e}_{2m}\}$	The unit vectors of $\underline{C}_m$ eigenframe
$f_c$	The curvature free energy density
$f_o$	The orientational free energy density
$F_o$	The orientational free energy
$g$	The genus of the surface
$H$	The mean curvature
$H_m$	The mean intrinsic curvature
$\underline{I}$	The Identity tensor
$I_n$	The Bessel function of n-th order
$k_B$	The Boltzmann constant
$k_1, k_2$	The elastic constants
$K$	The total Gaussian curvature
$m$	The topological charge
$m_{tot}$	The total sum of topological charges
$\vec{n}, \vec{n}_\perp$	The orthogonal unit vectors and eigenvectors of $\underline{Q}$
$\underline{M}$	The mismatch curvature tensor
$\underline{R}$	The rotation matrix
$s$	A distance along meridians
$\underline{Q}$	The nematic tensor order parameter
$Q$	The partition function of a single nanodomain

$x$	The measurement of differences between membrane principal curvatures
$T$	Temperature
$T_c$	The phase transition temperature between orientationally disordered and ordered phase
$Tr$	Trace
$w$	The elastic energy density
$w_0$	The minimal possible value of $w$
$\eta$	The average orientational degree of anisotropic nanodomains
$\vec{v}$	The outer unit normal
$\varphi$	The azimuthal angle
$\lambda$	The degree of ordering
$\chi$	The Euler-Poincare characteristic
$\xi$	The order parameter correlation length
$\omega$	The angle between the principal axes of tensors $\underline{C}_m$ and $\underline{C}$
$\theta$	The angel between $\vec{e}$ and $\vec{n}$
$\Delta F_c$	The free energy of the flexible membrane nanodomain
$\nabla_s$	The surface gradient operator

## I. Introduction

Influence of various parameters on biological membrane structure is of interest for years. Membrane shape changes are linked with various cellular processes of vital biological importance.

Structural reshaping might be provoked by varying external conditions (temperature, pressure, concentration...), changes in effective elasticity by adhering nanoparticles or colloids, by onset of orientational order within a biological membrane, or by some other means.

A membrane might exhibit an in-plane membrane surface orientational ordering.

Such ordering might arise due to tilting of lipid molecules relative to the normal of a membrane or in-plane averaged orientational ordering of lipid molecules due to their intrinsic anisotropic shape [1]-[3]. Besides the lipids and dimeric detergents the origin of anisotropic membrane components (nanodomains) might be also membrane embedded or membrane attached proteins [4]-[7].

Pioneering study of the impact of in-plane ordering on membrane shape was performed by MacKintosh and Lubensky [8]. Their mean-field theory suggested the coupling between in-plane ordering of membrane anisotropic components and membrane curvature could trigger membrane shape transitions. Further experimental and theoretical works demonstrated a rich variety of such changes.

For example, it was demonstrated in [6] and [9] that strongly anisotropic dimeric cationic amphiphiles induce tubular membrane budding while isotropic amphiphiles promote spherical membrane budding. Further studies [10] showed that in-plane ordering might suppress vesicle structures exhibiting neck-type profiles. On the other hand saddle-like membrane components may stabilize highly curved membrane necks [2],[5].

If tangential orientational ordering exists within a closed two-dimensional system then topological defects (TDs) in orientational order could unavoidable appear due to topological reasons [11]. The main topological characteristic of a topological defect is its topological charge  $m$ . The total sum of topological charges  $m_{\text{tot}}$  of all defects residing on a closed surface is a conserved quantity and is determined by a theorem of Poincare [12]. It claims that  $m_{\text{tot}}$  must equal the Euler-Poincare characteristic  $\chi=2(1-g)$  of the surface, which is determined by the total Gaussian curvature  $K$  of the surface.

The integer  $g$  is the genus of the surface, reflecting to the number of "handles" that the surface contains. For example, an object with the spherical topology corresponds to  $g=0$ , therefore  $m_{\text{tot}}=2$ .

Furthermore, spatial dependence of  $K$  could have strong impacts on position and even number of defects. It was demonstrated [13] that positive (negative)  $K$  attracts defects with positive (negative) topological charge  $m$ . It was also suggested that surfaces exhibiting both negative and positive Gaussian curvature might trigger unbinding of topological pairs defect - antidefects. The former and the latter correspond to  $m>0$  and  $m<0$ , respectively.

In this paper we present and compare two recently developed mesoscopic approaches which consider impact of membrane curvature on degree of in-plane orientational ordering. The plan of the paper is as follows.

In Sec. II we present the approach based on the mismatch curvature tensor. In Sec. III the modeling based on tensor orientational order parameter is presented. In the last section applicability of both approaches are discussed.

## II. Mismatch Curvature Tensor Approach

### II.1. Free Energy Density

It is assumed that a thin membrane consists of equal nanodomains. They are treated as two-dimensional anisotropic flexible plates of area  $a_0$  and their intrinsic shape is determined by the intrinsic curvature tensor commonly labeled by  $\underline{C}_m$ . The latter reflects average anisotropic character of membrane constituents [1],[2],[3],[9]. The interaction between nanodomains determines an actual membrane shape, which is locally given by the effective curvature tensor  $\underline{C}$ . These tensors are in their corresponding eigenframes determined by unit vectors  $\{\bar{e}_1, \bar{e}_2\}$  and  $\{\bar{e}_{1m}, \bar{e}_{2m}\}$  expressed as:

$$\underline{C}_m = C_{1m}(\bar{e}_{1m} \otimes \bar{e}_{1m}) + C_{2m}(\bar{e}_{2m} \otimes \bar{e}_{2m}) \quad (1)$$

$$\underline{C} = C_1(\bar{e}_1 \otimes \bar{e}_1) + C_2(\bar{e}_2 \otimes \bar{e}_2) \quad (2)$$

Here  $\otimes$  marks the tensorial product and  $C_{1m}, C_{2m}, C_1, C_2$  stand for principal curvatures. Both eigenframes are in general oriented along different directions. The misalignment of these tensors is quantified by the mismatch curvature tensor [2], [3], [9]:

$$\underline{M} = \underline{R}\underline{C}_m\underline{R}^{-1} - \underline{C} \quad (3)$$

The rotation matrix:

$$\underline{R} = (\bar{e}_1 \otimes \bar{e}_1 + \bar{e}_2 \otimes \bar{e}_2) \cos \omega + (\bar{e}_2 \otimes \bar{e}_1 - \bar{e}_1 \otimes \bar{e}_2) \sin \omega \quad (4)$$

determines the mutual rotation of the principal axes of tensors  $\underline{C}_m$  and  $\underline{C}$  by an angle  $\omega$  in the tangent plane of the membrane. It is assumed that the system aims to locally minimize value of  $\underline{M}$  and  $\underline{M}$  represents the key local quantity affecting the elastic energy density  $w$  per surface area  $a_0$  of a membrane. In the lowest approximation the  $w(\underline{M})$  dependence is expressed as a Taylor expansion up to the second order in powers of invariants of  $\underline{M}$ :

$$w = w_0 + \frac{k_1}{2}(\text{Tr}\underline{M})^2 + k_2 \text{Det}\underline{M} \quad (5)$$

here  $\text{Det}\underline{M}$  and  $\text{Tr}\underline{M}$  stand for determinant and trace of  $\underline{M}$ , respectively, while  $k_1$  and  $k_2$  are elastic constants.

The requirement  $w \geq 0$  imposes inequalities [14]:

$$k_2 < 0, \quad k_1 > -\frac{k_2}{2} \quad (6)$$

The quantity  $w_0$  equals minimal possible value of  $w$ .

For simplicity we henceforth set  $w_0=0$  and  $k_m = k_1 = |k_2|$ . It follows:

$$w = k_m \left( \begin{aligned} &(H - H_m)^2 + \\ &+ (D^2 - 2DD_m \cos(2\omega) + D_m^2) \end{aligned} \right) \quad (7)$$

where the mean curvature  $H$ , mean intrinsic curvature  $H_m$ , curvature deviator  $D$  and intrinsic curvature deviator  $D_m$  are defined as:

$$\begin{aligned} H &= \frac{C_1 + C_2}{2}, H_m = \frac{C_{1m} + C_{2m}}{2}, \\ D &= \frac{|C_1 - C_2|}{2}, D_m = \frac{|C_{1m} - C_{2m}|}{2} \end{aligned} \quad (8)$$

For  $D_m=0$  (i.e.  $C_{1m}=C_{2m}$ ) the expression Eq. (7) transforms into the Helfrich isotropic energy [15].

The free energy of the flexible membrane nanodomain  $\Delta F_c$  can be expressed as:

$$\Delta F_c = f_c a_0 = -k_B T \ln Q \quad (9)$$

where the subscript c refers to the curvature contribution.

The quantities  $f_c$ ,  $k_B$  and  $T$  stand for curvature free energy density, Boltzmann constant and temperature, respectively. The partition function of a single nanodomain is given by:

$$Q = \int_0^{2\pi} e^{-\frac{w a_0}{k_B T} d\omega} \quad (10)$$

Taking into account Eq. (7) it follows:

$$\begin{aligned} f_c &= k_m \left( (H - H_m)^2 + (D^2 + D_m^2) \right) + \\ &- k_B T \ln \left( I_0 \left( \frac{2k_m a_0 D D_m}{k_B T} \right) \right) \end{aligned} \quad (11)$$

and  $I_n$  labels the Bessel function of n-th order. Average orientational degree of anisotropic nanodomains can be obtained via equation:

$$\eta = \langle \cos(2\omega) \rangle = \frac{1}{Q} \int_0^{2\pi} \cos(2\omega) e^{-\frac{w a_0}{k_B T} d\omega} \quad (12)$$

The brackets  $\langle \dots \rangle$  mark ensemble averaging and  $\eta$  plays the role of order parameter.

It follows:

$$\eta = \frac{I_1(x)}{I_0(x)} \quad (13)$$

$$x = \frac{2k_m a_0 D D_m}{k_B T} \quad (14)$$

## II.2. Degree of Ordering

In Fig. 1 we plot  $\eta(x)$  dependence, where  $x$  measures differences between membrane principal curvatures. In the high temperature regime ( $x \sim 0$ , i.e.  $2k_m a_0 D D_m \gg k_B T$ ) one obtains  $\eta = \langle \cos(2\omega) \rangle \sim 0$  reflecting absence of orientational ordering. On the other hand in the low temperature regime ( $x \sim 1$ , i.e.  $2k_m a_0 D D_m \ll k_B T$ ) it follows  $\langle \cos(2\omega) \rangle^{(low)} \sim 1$ , revealing perfect alignment of nanodomain eigenframe along the curvature eigenframe.

Furthermore:

$$f_c^{(low)} = k_m \left( (H - H_m)^2 + (D - D_m)^2 \right) \quad (15)$$

The superscript <sup>(low)</sup> marks the low temperature regime. By comparing Eq. (7) and Eq. (15) we see that the latter expression corresponds to the situation where  $w$  exhibits minimal value, corresponding to "perfectly" oriented nanodomains.

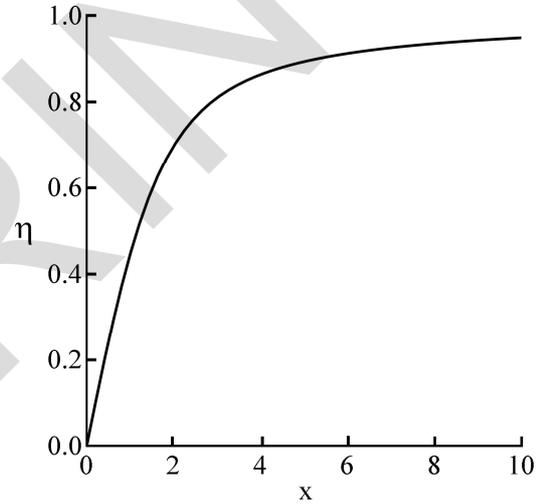


Fig. 1. Degree of local ordering  $\eta$  as a function of  $x = 2k_m a_0 D D_m / (k_B T)$

## III. Nematic Tensor Order Parameter Approach

### III.1. Free Energy Density

In the following we describe minimal mesoscopic theory describing orientational in-plane ordering of a membrane in terms of nematic tensor order parameter for a given membrane shape. Details are given in [16].

We assume that nanodomains lie on the local membrane tangent plane the orientation of which is given by its the outer unit normal  $\bar{v}$ . A temporal local orientation of a nanodomain is given by the unit vector  $\bar{e}$ . The corresponding tensor order parameter is defined as [16]:

$$\underline{Q} = \left\langle \bar{e} \otimes \bar{e} - \frac{1}{2} (I - \bar{v} \otimes \bar{v}) \right\rangle \quad (16)$$

where  $\underline{I}$  stands for the Identity tensor and  $Tr\underline{Q} = 0$ .

Alternatively, we can express the order parameter as

$$\underline{Q} = \lambda(\bar{n} \otimes \bar{n} - \bar{n}_\perp \otimes \bar{n}_\perp) \quad (17)$$

The orthogonal unit vectors  $\bar{n}$  and  $\bar{n}_\perp$  are eigenvectors of  $\underline{Q}$ , where  $\bar{v} = \bar{n} \times \bar{n}_\perp$ . The eigenvalue  $\lambda$  corresponding to the eigenvector  $\bar{n}$ , also referred to as nematic director field, can be expressed as:

$$\lambda = \bar{n} \cdot \underline{Q}\bar{n} = \left\langle (\bar{e} \cdot \bar{n})^2 - \frac{1}{2} \right\rangle = \frac{\langle \cos(2\theta) \rangle}{2} \quad (18)$$

where  $\bar{e} \cdot \bar{n} = \cos\theta$ . Furthermore,  $\bar{n}_\perp \cdot \underline{Q}\bar{n}_\perp = -\lambda$ . We relate  $\bar{n}$  to positive value of  $\lambda$ , where  $\lambda \in [0, 1/2]$ .

The corresponding orientational free energy density  $f_0$  can be expressed as a Landau-type expansion in terms of  $\underline{Q}$  taking into account symmetry allowed terms. In the lowest order approximation it is given by:

$$f_0 = \frac{A_0 t}{2} Tr\underline{Q}^2 + \frac{B}{2} (Tr\underline{Q})^2 + \frac{k}{2} |\nabla_s \underline{Q}|^2 \quad (19)$$

here  $t = (T - T_c)/T_c$  stands for the reduced temperature,  $T_c$  describes the phase transition temperature between orientationally disordered and ordered phase,  $A_0, B, k$  are material constants and  $\nabla_s$  marks the surface gradient operator.

In elastically undistorted bulk system the equilibrium degree of ordering in orientationally ordered phase is given by:

$$\lambda_b = \lambda_0 \sqrt{-t} \quad (20)$$

where  $\lambda_0 = \sqrt{A_0 / (2B)}$ . The competition between the condensation (the first two terms in Eq. (19)) and elastic (the last term in Eq. (19)) free energy contributions defines order parameter correlation length of the system, which is roughly given by:

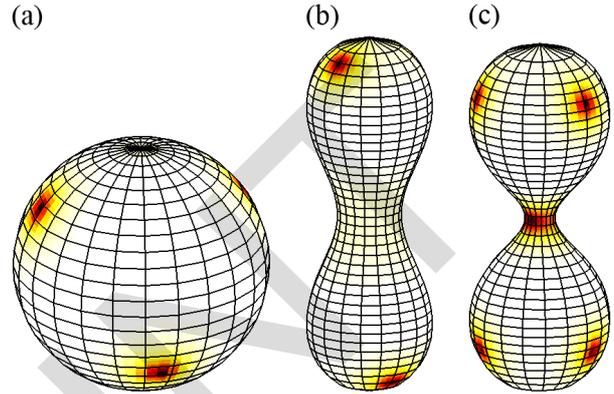
$$\xi \sim \frac{\xi_0}{\sqrt{|t|}} \quad (21)$$

and  $\xi_0 \sim \sqrt{k / A_0}$ .

### III.2. Degree of Ordering

In the following we show some qualitatively different orientational textures on membranes exhibiting spherical topology which are calculated by minimizing the orientational free energy  $F_0 = \oint f_0 da$  for a given membrane shape.

The integral is carried over the total surface of the membrane and  $da$  stands for an infinitesimal surface area. For simplicity we restrict to axially symmetric membrane. Technical details are given in [16]. In Fig. 2 we plot three different membrane shapes where degree of ordering  $\lambda$  is superimposed. Regions with white color exhibit degree of ordering comparable to  $\lambda_b$ . Within colored regions the degree of orientational ordering is essentially melted. These regions reveal existence of topological defects (TDs).



Figs. 2. Two-dimensional plot of  $\lambda$  superimposed on membrane shapes possessing spherical topology. Colored points reveal existence of topological defects

Relative position of defects, their number and core structure is better visualized by plotting degree of ordering in the  $(s, \varphi)$  plane, see Figs. 3. Here  $\varphi$  is the azimuthal angle and  $s$  measures a distance along meridians (the upper point in structures correspond to  $s=0$  and the lower point to the length  $s_0$ ). The corresponding director profiles are depicted in Figs.4.

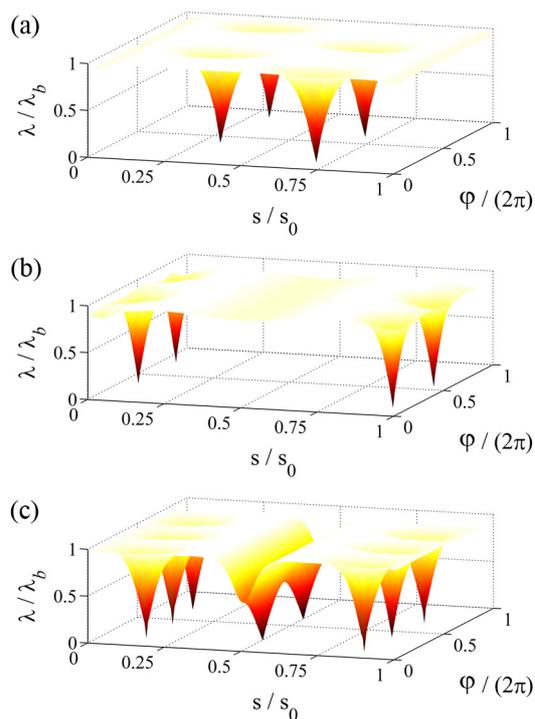
Within a spherical membrane (Figs. 2(a), 3(a), 4(a)) there are four TDs exhibiting topological charge  $m=1/2$ . These defects repeal each other and consequently they fall at the vertices of a tetrahedron in order to maximize their mutual separation [17].

Structures shown in Fig. 2(b) and Fig. 2(c) exhibit spatially dependent Gaussian curvature  $K$ . The latter is known to have similar impact on topological defects as electric field on electric charges. In Fig. 2(b) the central region exhibits  $K < 0$ .

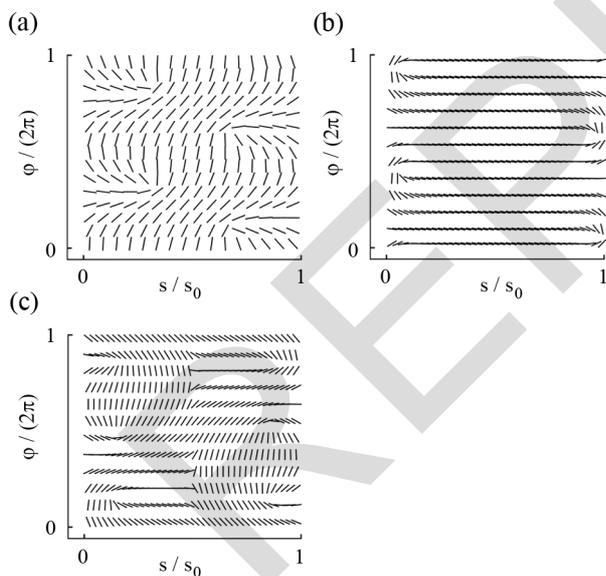
Consequently, TDs bearing  $m=1/2 > 0$  are pushed towards the poles of membranes. In structure shown in Fig. 2(c) elastic distortions in region where  $K < 0$  is strong enough to trigger unbinding of TDs. Two additional pairs of defects appear, where each pair consist of TDs bearing  $m=1/2$  and  $m=-1/2$ . Defects with  $m=1/2$  tend to assemble in the region exhibiting maximal value of  $K$ .

Their relative position compromises this tendency and their mutual repulsion.

On the other hand defects with  $m=-1/2$  assemble at the neck of the structure shown in Fig. 2(c), which exhibits most negative value of  $K$ .



Figs. 3. Two-dimensional plot of  $\lambda$  in the  $(\varphi, s)$  plane. There are four topological defects in (a) and (b) and eight in (c). The core size of defects is roughly given by the order parameter correlation length  $\xi$



Figs. 4. Two-dimensional plots of director profiles. Configurations in (a) and (b) possess four topological defects exhibiting topological charges  $m=1/2$ . In (c) there are six defects with  $m=1/2$  and two defects with  $m=-1/2$ . In all cases the total topological charge of structures equals two due to membrane's spherical topology

#### IV. Conclusion

In the paper we present two different approaches considering the impact of membrane's shape on its in-plane orientational ordering. Both assume that building blocks (nanodomains) exhibit the so called head-to-tail

symmetry. The first approach [2] is derived at a semi-microscopic level, where essential elastic property of an average nanodomain is given by its intrinsic curvature tensor. The latter determines locally favored membrane shape. Deviations from this reference are measured by the mismatch tensor  $\underline{M}$ , the symmetry invariants of which determine the membrane interaction energy  $w$ . The latter depends on the relative angle  $\omega$  between the intrinsic membrane curvature eigenframe and actual membrane curvature eigenframe.

Statistical averaging yields average degree of local ordering  $\eta = \langle \cos(2\omega) \rangle$  which depends on dimensionless quantity  $x = 2k_m a_0 D D_m / (k_B T)$ . In case of  $D=0$  or  $D_m=0$  or  $k_B T \rightarrow \infty$  it follows  $m=0$ , suggesting absence of preferred local field and consequently absence of ordering. On the other hand in the low temperature limit and for cases where both  $D$  and  $D_m > 0$  a local field is present, giving rise to finite degree of local ordering. Note that positive values of curvature deviators reflect difference of local principal curvatures. Using this approach we estimate only impact of local membrane conditions on average orientation of a nanodomain constituting a membrane. Furthermore, from the partition function curvature membrane free energy is derived. This approach does not take into account global topology of the problem. It only identifies semi-microscopic origin of local fields affecting in-plane ordering. In the second approach [16] one originates from local tensor order parameter  $\underline{Q}$ , revealing average degree of ordering at mesoscopic level. The corresponding elastic energy is constructed via Taylor expansion in  $\underline{Q}$  taking into account symmetry allowed terms. This approach takes into account global topology of the system. Derivation presented in [16] assumes fixed membrane shape. Furthermore, because of its mesoscopic character it does not take into account microscopic details. To simulate mutual influence of membrane curvature and orientational ordering symmetry allowed coupling terms between curvature tensor and tensor order parameter should be taken into account, where both  $\underline{C}$  and  $\underline{Q}$  are treated as variational parameters. These coupling terms introduce local field-type terms, one of which naturally emerges from the approach based on  $\underline{M}$ . This is the main goal of our future study.

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#### References

[1] T. Fischer, Bending stiffness of lipid bilayers. III. Gaussian curvature, *Journal de Physique II (France)*, Volume 2, 1992, Pages 337-343.  
 [2] V. Kralj-Iglič, B. Babnik, et al., Quadrupolar ordering of

- phospholipid molecules in narrow necks of phospholipid vesicles, *J. Stat. Phys.*, Volume 125, 2006, Pages 727-752.
- [3] Š. Perutkova, M. Daniel, et al., Elastic deformations in hexagonal phases studied by small angle X-ray diffraction and simulations, *Phys. Chem. Chem. Phys.*, Volume 13, 2011, Pages 3100-3107.
- [4] J.B. Fournier, Nontopological saddle-splay and curvature instabilities from anisotropic membrane inclusions, *Phys. Rev. Lett.*, Volume 76, 1996, Pages 4436-4439.
- [5] V. Kralj-Iglič, V. Heinrich, et al., Free energy of closed membrane with anisotropic inclusions, *Eur. Phys. J B*, Volume 10, 1999, Pages 5-8.
- [6] D. Kabaso, M. Lokar M., et al., Temperature and cholera toxin B are factors that influence formation of membrane nanotubes in RT4 and T24 urothelial cancer cell lines, *Int. J Nanomedicine*, Volume 6, 2011, Pages 495-509.
- [7] T. Baumgart, B.R. Capraro BR, et al., Thermodynamics and mechanics of membrane curvature generation and sensing by proteins and lipids, *Annu. Rev. Phys. Chem.* Volume 62, 1999, Pages 483-506
- [8] F.C. MacKintosh, T.C. Lubensky, Orientational order, topology, and vesicle shapes, *Phys. Rev. Lett.*, Volume 67, 1991, Pages 1169-1172.
- [9] V. Kralj-Iglič, A. Iglič, et al., Microtubes and nanotubes of a phospholipid bilayer membrane, *Journal of Physics A: Mathematical and General*, Volume 35, 2002, Pages 1533-1549.
- [10] A. Iglič, B. Babnik, et al., On the role of membrane anisotropy in the beading transition of undulated tubular membrane structures, *J. Phys. A: Math Gen.*, Volume 38, 2005, Pages 8527-8536.
- [11] N. Mermin, The topological theory of defects in ordered media, *Rev. Mod. Phys.*, Volume 51, 1979, Pages 591-648.
- [12] H. Poincaré, Mémoire sur les courbes définies par une équation différentielle, *J Math Pures Appl.*, Volume 2, 1886, Pages 151-217.
- [13] V. Vitelli, A.M. Turner, Anomalous coupling between topological defects and curvature, *Phys Rev. Lett.*, Volume 93, 2004, Pages 215301.
- [14] A. Iglič, M. Lokar, et al., Possible role of flexible red blood cell membrane nanodomains in the growth and stability of membrane nanotubes, *Blood Cells, Molecules and Diseases*, Volume 39, 2007, Pages 14-23.
- [15] W. Helfrich, Elastic properties of lipid bilayers: theory and possible experiments, *Z. Naturforsch. C*, Volume 28, 1973, Pages 693-703.
- [16] S. Kralj, R. Rosso, E.G. Virga, Curvature control of valence on nematic shells, *Soft Matter*, Volume 7, 2011, Pages 670-683.
- [17] V. Vitelli, D.R. Nelson, Nematic textures in spherical shells, *Phys. Rev. E*, Volume 74, 2006, Pages 021711-021721.

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